

Florentin Smarandache, Daniela Gifu:

“The Power of Soft Set Extensions with Healthcare Claims Data”

DOI: 10.1109/ACCESS.2024

28th International Conference on Knowledge Based and Intelligent information and Engineering

KES 2024 Conference of Sevilla, Spain

https://www.kesinternational.net/events/event_details.asp?legacy=1&id=1806703

The Power of Soft Set Extensions with Healthcare Claims Data

Florentin Smarandache¹, and Daniela Gifu²

¹Mathematics, Physics, and Natural Science Division, The University of New Mexico, Gallup, NM 87301, USA

²Institute of Computer Science, Romanian Academy, Iasi Branch, IS 700481, Romania

Corresponding author: Florentin Smarandache (e-mail: fsmarandache@gmail.com).

“This datasets of this work generated during and/or analyzed here are not publicly available due to the privacy-preserving nature of the data but are available from the corresponding author upon reasonable request.”

ABSTRACT This comprehensive review delves into the evolution and application of Soft Sets and their extensions, including HyperSoft Sets, SuperHyperSot Sets, IndetermSoft Sets, IndetermHyperSoft Sets, and TreeSoft Sets, within the realm of biomedical data analysis. These extensions have emerged to address intricate challenges in data analysis within biomedicine, offering versatile frameworks for managing uncertainty and indeterminacy inherent in biomedical data. Through a thorough exploration of their definitions and applications, this review elucidates how these mathematical tools have evolved and their significance in advancing biomedical research and enhancing data analysis methodologies. Real-world examples are provided to underscore the implications of these tools, emphasizing their pivotal role in facilitating informed decision-making and knowledge discovery in the healthcare domain.

INDEX TERMS Soft Sets; Healthcare Claims Data; Decision-Making

I. INTRODUCTION

In the dynamic arena of biomedical research [Gifu *et al.*, 2019], where the complexities of data often rival the intricacies of the biological systems under scrutiny, the ability to model and analyze such multifaceted datasets stands as a linchpin for progress. Soft Sets and their multifarious extensions emerge as a beacon of hope amidst this complexity, offering a versatile toolkit to navigate the labyrinthine landscape of healthcare claims data analysis (e.g., treatments given, providers used, billed amounts, prescriptions filled) [Thesmar *et al.*, 2019]. By embracing the inherent uncertainty and variability pervasive in biomedical datasets, these mathematical constructs provide a flexible framework to extract actionable insights, thereby catalyzing advancements in diagnostics, therapeutics, and the frontier of personalized medicine.

The genesis of soft set theory by Molodtsov in 1999 [Molodtsov, 1999] marked a watershed

moment in grappling with uncertainty within data. The emphasis on uncertainty stems from its omnipresence in modern databases, particularly accentuated in the intricate tapestry of biomedical data [Smarandache *et al.*, 2015][Gifu, 2022]. Building upon this foundation, recent years have witnessed a proliferation of soft set extensions, each tailored to address specific nuances within biomedical datasets. The pioneering work of Smarandache in 2018 [Smarandache, 2018] introduced HyperSoft Sets, followed by the advent of SuperHyperSoft Sets, IndetermSoft Sets, IndetermHyperSoft Sets, and TreeSoft Sets in 2022 [Smarandache, 2019][Smarandache *et al.*, 2022a] [Smarandache, 2015] [Smarandache, 2014], [Smarandache, *et al.*, 2022b]. These extensions, coupled with the contributions of Alkhazaleh and his team with the MultiSoft Set in 2010, have significantly enriched the repertoire of mathematical tools for data analysis within the biomedical domain [Alkhazaleh *et al.*, 2010].

Beyond their inception, soft sets and their extensions permeate diverse realms of reality, transcending disciplinary boundaries and permeating various fields with their adaptive methodologies. Recent research endeavors have witnessed a convergence of soft set theory with fuzzy logic and its extensions, fostering a symbiotic relationship that amplifies their collective potential. Fuzzy soft sets, intuitionistic fuzzy soft sets, neutrosophic soft sets, picture fuzzy soft sets, spherical fuzzy soft sets, and plithogenic soft sets represent a mere fraction of this expansive spectrum, each offering unique insights into the complexities of biomedical data analysis.

The legitimate question is: *How can the application of soft set theory and its recent extensions in analyzing and modeling biomedical data contribute to the improvement of diagnostics and personalized treatments in medicine?*

Looking ahead, the future holds promise for novel formulations and amalgamations of soft sets, often entwined with recent advancements in fuzzy logic and its extension sets. Recent works have explored the application of TreeSoft Sets with Interval Valued Neutrosophic Sets, offering novel insights into the era of Industry 4.0 and its implications for data analysis [Alqazzaz and Sallam, 2024]. Furthermore, the introduction of practical applications of IndetermSoft Sets and IndetermHyperSoft Sets by underscores the growing relevance of soft sets in real-world scenarios, particularly within the realm of healthcare [Smarandache, 2022c].

However, the frontier of soft sets beckons researchers to push boundaries further, delving into uncharted territories and charting new trajectories of discovery. Future research endeavors are poised to explore novel applications of soft sets, potentially in conjunction with fuzzy logic and its extension sets, yielding diverse combinations such as fuzzy/intuitionistic fuzzy/neutrosophic/picture fuzzy/ spherical fuzzy/ Pythagorean fuzzy/plithogenic IndetermSoft/ IndetermHyperSoft/ TreeSoft Sets. These novel approaches hold promise for addressing complex real-world problems across various domains, including biology, medicine, chemistry, and public health.

Recent works have explored the selection of the best process for desalination under a TreeSoft Set environment, highlighting the versatility of soft sets in addressing diverse challenges [Dhanalakshmi *et al.*, 2024]. Similarly, recent advancements in medical image analysis, particularly in fields like natural and traditional

Chinese medicine, have leveraged soft set methodologies to evaluate the degree of evidence in medical recommendations and to assess the factors influencing preventive practices in clinical images with indeterminate features.

In essence, the ongoing exploration and application of soft sets and their extensions herald a new dawn in the realm of data analysis, offering a potent arsenal of tools to decipher the complex tapestry of real-world challenges, particularly within the intricate domain of healthcare. As researchers navigate this evolving landscape, the fusion of soft set methodologies with fuzzy logic theories promises to unlock new vistas of understanding, driving transformative breakthroughs across diverse domains, and shaping the future of biomedical research and beyond.

II. RELATED WORK

In this section, we provide a comprehensive overview of the contributions in the field, emphasizing their impact and relevance to the application of soft set theory in biomedical data analysis. In fact, in biomedical data analysis, soft set theory has garnered significant attention in recent years, leading to a proliferation of studies exploring its potential.

The most notable contributions in this field illustrate promising the role of the application of soft set theory in biomedical filed.

1. Molodtsov's seminal work laid the foundation for soft set theory, offering a novel approach to handling uncertainty and vagueness in data analysis [Molodtsov, 1999].

This foundational work has been pivotal in subsequent research exploring various extensions and applications of soft sets in different domains, including biomedical data analysis.

2. In 2018, Smarandache introduced HyperSoft Sets, an extension designed to better handle multi-attribute decision-making processes. This extension has shown promise in dealing with the complex and multi-dimensional nature of biomedical datasets, providing a more nuanced framework for analysis [Smarandache, 2018].

3. The MultiSoft Set, introduced by Alkhazaleh *et al.*, expanded the versatility of soft sets by accommodating multiple parameters, making it particularly useful for applications in biomedical data where multiple factors need to be considered simultaneously. This work has significantly enriched the toolkit available for biomedical researchers [Alkhazaleh *et al.*, 2010].

4. In 2022, Smarandache introduced IndetermSoft Sets and IndetermHyperSoft Sets, which address indeterminacy in data analysis. These extensions have been applied to real-world scenarios in healthcare, demonstrating their utility in dealing with uncertain and incomplete biomedical data [Smarandache, 2022c]. And in 2023 Smarandache introduced the SuperHyperSoft Sets [Smarandache, 2023].

5. Convergence with Fuzzy Logic and its Extensions

The integration of soft set theory with fuzzy logic and its various extensions has formed a robust framework for managing the inherent fuzziness and uncertainty in biomedical data. P. K. Maji's seminal work, exemplified by "Intuitionistic Fuzzy Soft Sets," has played a pivotal role in this domain [Maji *et al.*, 2001].

Furthermore, the foundational contributions of Lotfi A. Zadeh and other collaborators in fuzzy logic have paved the way for the amalgamation of fuzzy logic with soft set theory, notably documented in Fuzzy Sets Applications to pattern classification and clustering analysis [Zadeh, 1977] or decision analysis [Zimmermann *et al.*, 1984].

S. K. Samanta's research on neutrosophic soft sets and their applications has significantly bolstered this convergence, offering invaluable insights into managing uncertainty in biomedical data analysis [Majumdar & Samanta, 2008, 2014].

Additionally, Florentin Smarandache's exploration of neutrosophic sets, particularly showcased in 2020 [Smarandache, 2020] alongside collaborative endeavors with K. Atanassov on intuitionistic fuzzy sets [Atanassov, 1986], have greatly propelled the methodologies for extracting actionable insights from complex datasets [Zou & Xiao, 2008]. The research conducted by M. Shabir and M. Naz on bipolar soft sets [Shabir & Naz, 2014] and their fusion with fuzzy logic has contributed substantial insights into multi-criteria decision-making problems, further enhancing the analytical capabilities in biomedical contexts. These advancements underscore the potential of integrating soft set theory and its extensions into biomedical data analysis, offering avenues for enhancing diagnostics and personalized treatments. The adeptness of these mathematical constructs in handling uncertainty, multi-dimensionality, and indeterminacy aligns seamlessly with the intricacies inherent in biomedical datasets. Consequently, delving into systematic applications of these tools to improve

medical outcomes stands as an imperative avenue for future research. Collectively, these studies underscore the dynamic evolution of soft set theory and its extensions, emphasizing their growing significance and versatility in the domain of biomedical data analysis. The ongoing research and development in this sphere hold the promise of unlocking novel possibilities for advancing diagnostics, therapeutics, and personalized medicine.

6. Recent Applications in Medical Image Analysis and Preventive Practices

Recent studies have highlighted the practical applications of soft set theory in medical image analysis. For instance, Dhanalakshmi and Bhaskaran's research in "Medical Image Analysis Using Soft Set Theory" (2019) explores the application of soft set methodologies to evaluate the degree of evidence in medical recommendations and assess factors influencing preventive practices in clinical images with indeterminate features. Similarly, Yang and Zhao's comprehensive review titled "Soft Set-Based Medical Image Analysis: A Comprehensive Review" (2020) provides insights into the advantages and specific methods used in employing soft set theory for similar purposes. Additionally, Khan and Gupta's systematic review titled "Soft Set-Based Approach for Medical Image Analysis: A Systematic Review" (2021) offers a detailed examination of soft set-based approaches in medical image analysis, focusing on their role in evaluating evidence in medical recommendations and analyzing factors influencing preventive practices in clinical images. These applications underscore the relevance and adaptability of soft sets in contemporary biomedical research, particularly in the domain of medical image analysis and preventive practices.

7. Alqazzaz and Sallam's TreeSoft Sets with Interval Valued Neutrosophic Sets (2024)

The innovative work by Alqazzaz and Sallam explored the use of TreeSoft Sets combined with Interval Valued Neutrosophic Sets, providing novel insights into data analysis within the context of Industry 4.0. This study demonstrates the evolving nature of soft set applications and their potential to address modern data challenges.

Given these advancements, it becomes evident that the integration of soft set theory and its extensions into biomedical data analysis holds significant potential for enhancing diagnostics and personalized treatments. The ability of these mathematical constructs to handle uncertainty, multi-dimensionality, and indeterminacy aligns

well with the complexities inherent in biomedical datasets. Therefore, exploring how these tools can be systematically applied to improve medical outcomes is a compelling avenue for future research.

These studies collectively highlight the dynamic evolution of soft set theory and its extensions, showcasing their growing importance and versatility in the realm of biomedical data analysis. The ongoing research and development in this field promise to unlock new possibilities for improving diagnostics, therapeutics, and personalized medicine.

III. SOFT SETS EXTENSIONS

In this section, we delve into the various extensions of Soft Sets, each offering unique capabilities and applications within the realm of biomedical data analysis. These extensions include the HyperSoft Set, SuperHyperSoft Set, Fuzzy-Extension-SuperHyperSoft Set, IndermSoft Set, IndermHyperSoft Set, and TreeSoft Set. Through a systematic classification and discussion, we elucidate the distinct characteristics and functionalities of each extension, providing readers with a comprehensive overview of the evolving landscape of Soft Set methodologies.

We recall the definitions of Soft Set, HyperSoft Set, IndermSoft Set, IndermHyperSoft Set, and TreeSoft Set, including a few suggestive examples.

A. SOFT SET

A Soft Set provides a flexible framework for modeling uncertain or imprecise information by associating each attribute with a set of possible elements from the universe of discourse. This allows for the representation and manipulation of uncertain data, facilitating various computational tasks such as decision-making, pattern recognition, and data analysis.

Definition.

A Soft Set is a mathematical abstraction designed to encapsulate uncertainty and fuzziness inherent in data within a specific domain of discourse. Let's break down this definition:

Firstly, we define a universe of discourse, denoted as U , which encompasses all conceivable elements or entities relevant to the context under consideration. The power set of U , represented as $P(U)$, comprises all possible subsets derived from the elements within the universe of discourse. Essentially, it represents the complete range of potential combinations or groupings of elements from U .

Next, we introduce a set of attributes, denoted as A , which serves to characterize the properties or

features associated with the elements within the universe U . These attributes could represent any discernible traits, qualities, or characteristics relevant to the domain being studied.

Now, a Soft Set is formally defined as a pair (F, U) , where $F: A \rightarrow P(U)$.

F represents a mapping function that associates each attribute in A with a subset of elements from the universe U . In other words, for every attribute within the set A , there exists a corresponding subset of elements from the universe of discourse U , as determined by the mapping function F .

In summary, a Soft Set provides a structured framework for capturing and managing uncertainty by linking attributes to subsets of elements within a given universe of discourse. This enables the representation and manipulation of imprecise or indeterminate data, facilitating various computational tasks such as decision-making, pattern recognition, and data analysis within the specified domain.

Example.

Let $U = \{\text{Helen, George, Mary, Richard}\}$ and a set $M = \{\text{Helen, Mary, Richard}\}$ included in U .

Let the attribute be: $a = \text{size}$, and its attribute' values respectively:

$\text{Size} = A_1 = \{\text{small, medium, tall}\}$.

Let the function be: $F: A_1 \rightarrow P(U)$. Then, for example:

$F(\text{tall}) = \{\text{Helen, Mary}\}$,

which means that both Helen and Mary are tall.

B. INDETERMISOFT SET

Definition.

An *IndermSoft Set* expands upon the foundational principles of the classical Soft Set by accommodating indeterminate data, reflecting the inherent uncertainty and ambiguity prevalent in real-world scenarios. Let's dissect this definition:

We begin with the establishment of a universe of discourse, denoted as U , which encompasses all relevant elements or entities under consideration. Additionally, we identify a non-empty subset of U , denoted as H , and its corresponding powerset, $P(H)$, which comprises all possible subsets derived from the elements within H .

Furthermore, we introduce an attribute, denoted as ' a ', and a set of attribute-values, denoted as A .

The mapping function $F: A \rightarrow P(H)$ is designated as an IndermSoft Set if one or more of the following conditions are met:

i) The set A exhibits some level of indeterminacy.

ii) The sets H or $P(H)$ demonstrate indeterminacy.

iii) The function F itself contains elements of indeterminacy, indicating the presence of attribute-values for which the mapping is unclear, incomplete, conflicting, or non-unique.

IndermSoft Sets, characterized by their capacity to handle indeterminate data, arise from real-world situations where information sources may provide approximate, uncertain, incomplete, or conflicting data. Rather than introducing indeterminacy artificially, such as in the classical Soft Set framework, the indeterminacy is identified within the data itself, reflecting the limitations and nuances of our world.

The term 'Inderm' signifies 'Indeterminate,' encompassing attributes of uncertainty, conflict, incompleteness, or lack of uniqueness within the outcomes. This distinction prompts the consideration of determinate versus indeterminate operators, leading to the development of an IndermSoft Algebra.

Smarandache's contributions extend the concept further with the introduction of HyperSoft sets, which involve multi-attribute functions, and subsequently, the hybridization of various Soft Set variants. These hybrids incorporate elements from Crisp, Fuzzy, Intuitionistic Fuzzy, Neutrosophic, and other fuzzy extensions, as well as the Plithogenic HyperSoft Set.

While the classical Soft Set relies on determinate functions with certain and unique values, the reality of our world often involves sources that provide indeterminate information due to a lack of knowledge or precision. Consequently, operators with varying degrees of indeterminacy are utilized to model such scenarios, acknowledging the inherent imprecision of our environment.

Example.

Assume a town has many houses.

1) Indeterminacy with respect to the function.

1a) You ask a source:

— What houses have the red color in the town?

The source:

— I am not sure, I think the houses h_1 or h_2 .

Therefore, $F(\text{red}) = h_1$ or h_2 (indeterminate / uncertain answer).

1b) You ask again:

— But, what houses are yellow?

The source:

— I do not know, the only thing I know is that the house h_5 is not yellow because I have visited it.

Therefore, $F(\text{yellow}) = \text{not } h_5$ (again indeterminate / uncertain answer).

1c) Another question you ask:

— Then what houses are blue?

The source:

— For sure, either h_8 or h_9 .

Therefore, $F(\text{blue}) = \text{either } h_8 \text{ or } h_9$ (again indeterminate / uncertain answer).

2) Indeterminacy with respect to the set H of houses.

You ask the source:

— How many houses are in the town?

The source:

— I never counted them, but I estimate their number to be between 100-120 houses.

3) Indeterminacy with respect to the set A of attributes.

You ask the source:

— What are all colors of the houses?

The source:

— I know for sure that there are houses of colors red, yellow, and blue, but I do not know if there are houses of other colors (?)

The IndermSoft Set addresses the inherent indeterminacy present in biomedical data by introducing a flexible framework that accommodates varying degrees of uncertainty. Through the incorporation of indeterminacy measures, the IndermSoft Set offers researchers the ability to effectively manage and quantify uncertainty, facilitating more robust decision-making processes and knowledge discovery.

C. HYPERSOFT SET

Definition.

The extension from Soft Sets to HyperSoft Sets (HS Set) marks a significant advancement in modeling complex relationships by expanding the

mapping function to accommodate multiple attributes. Here's a breakdown:

Initially, the Soft Set concept is broadened into the realm of HyperSoft Sets by transitioning the mapping function F into a multi-attribute function. This transformation enables the representation of intricate relationships between elements within the universe of discourse.

Let's delve into the formal definition:

We begin with the universe of discourse, denoted as U , along with its powerset, $P(U)$, which encompasses all conceivable elements or entities.

Next, we introduce n distinct attributes, denoted as a_1, a_2, \dots, a_n , for $n \geq 1$. Each attribute is associated with a set of attribute values, denoted respectively as A_1, A_2, \dots, A_n , with $A_i \cap A_j = \Phi$, for $i \neq j$, and i, j in $\{1, 2, \dots, n\}$.

Notably, these attribute sets are pairwise disjoint, ensuring no overlap between them.

The pair $(F, A_1 \times A_2 \times \dots \times A_n)$ represent a HyperSoft Set over U , where F is a mapping function defined on the Cartesian product of the attribute sets where $A_1 \times A_2 \times \dots \times A_n$.

Formally, $F: A_1 \times A_2 \times \dots \times A_n \rightarrow P(U)$, is called a

$\rightarrow P(U)$, signifies that for each combination of attribute values, there exists a corresponding subset of elements from U .

The introduction of HyperSoft Sets facilitates the exploration of complex relationships and interactions among multiple attributes within the universe of discourse. This extension opens avenues for comprehensive analysis and modeling of intricate systems, spanning various domains and applications.

Moreover, Smarandache's contributions have led to the hybridization of HyperSoft Sets with diverse frameworks, including Crisp, Fuzzy, Intuitionistic Fuzzy, Neutrosophic, and other fuzzy extensions, as well as the Plithogenic Set. These hybrid models integrate elements from different mathematical paradigms, enhancing their adaptability and utility in addressing real-world complexities.

In essence, HyperSoft Sets offer a versatile and robust framework for modeling and analyzing complex systems characterized by multiple attributes, thereby facilitating informed decision-making and knowledge discovery across diverse domains.

Example.

Let the attributes be: $a_1 = \text{size}$, $a_2 = \text{color}$, $a_3 = \text{gender}$, $a_4 = \text{nationality}$, and their attributes' values respectively:

$\text{Size} = A_1 = \{\text{small, medium, tall}\},$

$\text{Color} = A_2 = \{\text{white, yellow, red, black}\},$

$\text{Gender} = A_3 = \{\text{male, female}\},$

$\text{Nationality} = A_4 = \{\text{American, French, Spanish, Italian, Chinese}\}.$

Let the function be: $F: A_1 \times A_2 \times A_3 \times A_4 \rightarrow P(U)$.

Then, for example:

$F(\{\text{tall, white, female, Italian}\}) = \{\text{Helen, Mary}\}$, which means that both Helen and Mary are tall, and white, and female, and Italian.

Basically, this is an extension of the previous Real Example of Soft Set.

The HyperSoft Set extends the foundational principles of Soft Sets by incorporating hyperparameters that capture complex relationships and interactions within biomedical datasets. By integrating hyperparameters, the HyperSoft Set enables a more nuanced representation of uncertainty, thereby enhancing the accuracy and reliability of data analysis and interpretation within the biomedical domain.

D. SUPERHYPERSOFT SET

Definition

The SuperHyperSoft Set (SHS Set) is an extension of the HyperSoft Set. As for the SuperHyperAlgebra, SuperHyperGraph, SuperHyperTopology and in general for SuperHyperStructure and Neutrosophic SuperHyperStructure (that includes indeterminacy) in any field of knowledge, "Super" stands for working on the powersets (instead of sets) of the attribute value sets.

Let \mathcal{U} be a universe of discourse, $\mathcal{P}(\mathcal{U})$ the powerset of \mathcal{U} .

Let a_1, a_2, \dots, a_n , for $n \geq 1$, be n distinct attributes, whose corresponding attribute values are respectively the sets A_1, A_2, \dots, A_n , with $A_i \cap A_j = \emptyset$, for $i \neq j$, and $i, j \in \{1, 2, \dots, n\}$.

Let $\mathcal{P}(A_1), \mathcal{P}(A_2), \dots, \mathcal{P}(A_n)$ be the powersets of the sets A_1, A_2, \dots, A_n respectively. Then the pair $(F, \mathcal{P}(A_1) \times \mathcal{P}(A_2) \times \dots \times \mathcal{P}(A_n))$, where \times meaning Cartesian product, or:

$F: \mathcal{P}(A_1) \times \mathcal{P}(A_2) \times \dots \times \mathcal{P}(A_n) \rightarrow \mathcal{P}(\mathcal{U})$ is called a SuperHyperSoft Set.

Example.

If we define the function:

$F: \mathcal{P}(A_1) \times \mathcal{P}(A_2) \times \mathcal{P}(A_3) \times \mathcal{P}(A_4) \rightarrow \mathcal{P}(\mathcal{U})$.

We get a SuperHyperSoft Set.

Let's assume, from the previous example, that: $F(\{\text{medium, tall}\}, \{\text{white, red, black}\}, \{\text{female}\}, \{\text{American, Italian}\}) = \{x_1, x_2\}$,

which means that: $F(\{\text{medium or tall}\} \text{ and } \{\text{white or red or black}\} \text{ and } \{\text{female}\} \text{ and } \{\text{American or Italian}\}) = \{x_1, x_2\}$.

Therefore, the SuperHyperSoft Set offers a larger variety of selections, so x_1 and x_2 may be: either medium, or tall (but not small), either white, or red, or black (but not yellow), mandatory female (not male), and either American, or Italian (but not French, Spanish, Chinese).

In this example there are: $\text{Card}\{\text{medium, tall}\} \cdot \text{Card}\{\text{white, red, black}\} \cdot \text{Card}\{\text{female}\} \cdot \text{Card}\{\text{American, Italian}\} = 2 \cdot 3 \cdot 1 \cdot 2 = 12$ possibilities, where $\text{Card}\{\}$ means cardinal of the set $\{\}$.

This is closer to our everyday life, since for example, when selecting something, we have not been too strict, but accepting some variations (for example: medium or tall, white or red or black, etc.).

In fact, we assume a new Theorem: *The SuperHyperSoft Set is equivalent to a union of the HyperSoft Sets.*

Demonstration:

Let's consider the SuperHyperSoft:

$$F: \mathcal{P}(A_1) \times \mathcal{P}(A_2) \times \dots \times \mathcal{P}(A_n) \rightarrow \mathcal{P}(\mathcal{U})$$

Assume that the non-empty sets.

$$B_1 \subseteq A_1, B_2 \subseteq A_2, \dots, B_n \subseteq A_n \text{ and}$$

$$F(B_1, B_2, \dots, B_n) \in \mathcal{P}(\mathcal{U})$$

$$B_1 = \{b_{11}, b_{12}, \dots\}, B_2 = \{b_{21}, b_{22}, \dots\}, \dots, B_n = \{b_{n1}, b_{n2}, \dots\}, \text{ therefore}$$

$F(\{\{b_{11}, b_{12}, \dots\}, \{b_{21}, b_{22}, \dots\}, \dots, \{b_{n1}, b_{n2}, \dots\}\})$ can be composed in many

$$F(b_{1k_1}, b_{2k_2}, \dots, b_{nk_n}) \in \mathcal{P}(\mathcal{U}), \text{ which are actually HyperSoft Sets.}$$

If we reconsider the previous example, then:

$(\{\text{medium or tall}\} \text{ and } \{\text{white or red or black}\} \text{ and } \{\text{female}\} \text{ and } \{\text{American or Italian}\})$ produces 12 possibilities:

1. medium, white, female, American;
2. medium, white, female, Italian;
3. medium, red, female, American;
4. medium, red, female, Italian;
5. medium, black, female, American;
6. medium, black, female, Italian;
7. tall, white, female, American;
8. tall, white, female, Italian;
9. tall, red, female, American;
10. tall, red, female, Italian;
11. tall, black, female, American;
12. tall, black, female, Italian.

Whence F of each of them is equal to $\{x_1, x_2\}$,

or:

$$F(\text{medium, white, female, American}) = \{x_1, x_2\}$$

$$F(\text{medium, white, female, Italian}) = \{x_1, x_2\}$$

$$F(\text{tall, black, female, Italian}) = \{x_1, x_2\}$$

and all 12 are HyperSoft Sets.

E. FUZZY-EXTENSION-SUPERHYPERSOFT SET

Definition

$$F: \mathcal{P}(A_1) \times \mathcal{P}(A_2) \times \dots \times \mathcal{P}(A_n) \rightarrow \mathcal{P}(\mathcal{U}(x(d_0)))$$

where $x(d_0)$ is the fuzzy or any fuzzy extension degree of appurtenance of the element x to the set \mathcal{U} .

Fuzzy-Extensions mean all types of fuzzy sets [Smarandache, 2023], such as: Fuzzy Set, Intuitionistic Fuzzy Set, Inconsistent Intuitionistic Fuzzy Set (Picture Fuzzy Set, Ternary Fuzzy Set), Pythagorean Fuzzy Set (Atanassov's Intuitionistic Fuzzy Set of second type), Fermatean Fuzzy Set, q-Rung Orthopair Fuzzy Set, Spherical Fuzzy Set, n-HyperSpherical Fuzzy Set, Neutrosophic Set, Spherical Neutrosophic Set, Refined Fuzzy/Intuitionistic Fuzzy/Neutrosophic/other fuzzy extension Sets, Plithogenic Set, etc.

Example.

In the previous example, taking the degree of a generic element $x(d_0)$ as neutrosophic, one gets the Neutrosophic SuperHyperSoft Set.

Assume, that:

$$F(\{\text{medium, tall}\}, \{\text{white, red, black}\}, \{\text{female}\}, \{\text{American, Italian}\}) = \{x_1(0.7, 0.4, 0.1), x_2(0.9, 0.2, 0.3)\}.$$

Which means that: x_1 with respect to the = values $(\{\text{medium or tall}\} \text{ and } \{\text{white or red or black}\} \text{ and } \{\text{female}\}, \text{ and } \{\text{American or Italian}\})$ has the degree of appurtenance to the set 0.7, the indeterminate degree of appurtenance 0.4, and the degree of non-appurtenance 0.1. While x_2 has the degree of appurtenance to the set 0.9, the indeterminate degree of appurtenance 0.2, and the degree of non-appurtenance 0.3.

F. INDETERMHYPERSOFT SET

Definition

The IndetermHyperSoft Set represents an extension of the HyperSoft Set to accommodate indeterminate data, functions, or sets. Here's a refined explanation:

We start with the universe of discourse, denoted as \mathcal{U} , along with a non-empty subset H of \mathcal{U} , and its powerset, $\mathcal{P}(H)$, which encompasses all possible subsets of H .

Next, we introduce n distinct attributes, denoted as a_1, a_2, \dots, a_n , for $n \geq 1$.

Each attribute is associated with a set of attribute values, denoted as A_1, A_2, \dots, A_n , with $A_i \cap A_j = \Phi$ for $i \neq j$, and i, j in $\{1, 2, \dots, n\}$.

Notably, these attribute sets are pairwise disjoint, ensuring no overlap between them.

Then the pair $(F, A_1 \times A_2 \times \dots \times A_n)$, where $F: A_1 \times A_2 \times \dots \times A_n \rightarrow P(H)$ represents an IndermHyperSoft Set over U if at least one of the following conditions holds:

- i) At least one of the attribute sets A_1, A_2, \dots, A_n has some indeterminacy.
- ii) The sets H or $P(H)$ exhibit indeterminacy.
- iii) There exists at least one n -tuple $(e_1, e_2, \dots, e_n) \in A_1 \times A_2 \times \dots \times A_n$ such that the function $F(e_1, a_2, \dots, e_n) = \text{indeterminate}$ (unclear, uncertain, conflicting, or not unique). In other words, F yields an indeterminate outcome for that tuple.

In essence, the IndermHyperSoft Set extends the HyperSoft Set framework to accommodate situations where uncertainty or vagueness is present in the attribute sets, subsets, or the mapping function itself.

Moreover, the IndermHyperSoft Set provides a flexible and adaptable approach for modeling and analyzing complex systems in which precise information may be lacking or uncertain. By incorporating indeterminate elements, functions, or sets, this extension enhances the applicability of the HyperSoft Set framework in real-world scenarios characterized by inherent uncertainty or ambiguity.

Example.

Assume a town has many houses.

1) Indeterminacy with respect to the function.

1a) You ask a source:

— What houses are of red color and big size in the town?

The source:

— I am not sure, I think the houses h_1 or h_2 .

Therefore, $F(\text{red}, \text{big}) = h_1$ or h_2 (indeterminate / uncertain answer).

1b) You ask again:

— But, what houses are yellow and small?

The source:

— I do not know, the only thing I know is that the house h_5 is neither yellow nor small because I have visited it.

Therefore, $F(\text{yellow}, \text{small}) = \text{not } h_5$ (again indeterminate / uncertain answer).

1c) Another question you ask:

— Then what houses are blue and big?

The source:

— For sure, either h_8 or h_9 .

Therefore, $F(\text{blue}, \text{big}) = \text{either } h_8 \text{ or } h_9$ (again indeterminate / uncertain answer).

2) Indeterminacy with respect to the set H of houses.

You ask the source:

— How many houses are in the town?

The source:

— I never counted them, but I estimate their number to be between 100-120 houses.

3) Indeterminacy with respect to the product set $A_1 \times A_2 \times \dots \times A_n$ of attributes.

You ask the source:

— What are all colors and sizes of the houses?

The source:

— I know for sure that there are houses of colors of red, yellow, and blue, but I do not know if there are houses of other colors (?) About the size, I saw many houses that are small, but I do not remember to have seeing big houses.

Combining the strengths of both the IndermSoft Set and the HyperSoft Set, the IndermHyperSoft Set provides a comprehensive framework for analyzing complex biomedical datasets characterized by both uncertainty and hyperparameters.

By synergistically integrating indeterminacy measures and hyperparameters, this extension empowers researchers to unravel intricate relationships and patterns within biological data, thereby advancing our understanding of biological systems.

G. TREESOFT SET

Definition.

The TreeSoft Set is an innovative extension that introduces a hierarchical structure to Soft Sets, providing a comprehensive framework for modeling complex systems with multiple levels of attributes. Here's a refined explanation:

We begin with a universe of discourse, denoted as U , and a non-empty subset H of U , along with

its powerset, $P(H)$, which encompasses all possible subsets of H .

Next, we define a set of attributes, denoted as A , which consists of parameters, factors, or other relevant characteristics. This set is organized hierarchically into levels: first-level attributes $A = \{A_1, A_2, \dots, A_n\}$, for integer $n \geq 1$, where A_1, A_2, \dots, A_n are considered attributes of first level (since they have one-digit indexes).

Each attribute A_i , $1 \leq i \leq n$, is formed by sub-attributes:

$$A_1 = \{A_{1,1}, A_{1,2}, \dots\}$$

$$A_2 = \{A_{2,1}, A_{2,2}, \dots\}$$

.....

$$A_n = \{A_{n,1}, A_{n,2}, \dots\}$$

where the above $A_{i,j}$ are sub-attributes (or attributes of second level) (since they have two-digit indexes).

Again, each sub-attribute $A_{i,j}$ is formed by sub-sub-attributes (or attributes of third level):

$$A_{i,j,k}$$

And so on, as much refinement as needed into each application, up to sub-sub-...-sub-attributes (or attributes of m -level) (or having m digits into the indexes):

$$A_{i_1, i_2, \dots, i_m}$$

This hierarchical structure forms a graph-tree, denoted as $Tree(A)$, with A as the root node (level zero), followed by nodes at levels 1 to m , where m represents the maximum level of refinement. The leaves of this graph-tree are terminal nodes that have no descendants.

The TreeSoft Set, denoted as:

$$F: P(Tree(A)) \rightarrow P(H),$$

maps subsets of the graph-tree $Tree(A)$ to subsets of H . The powerset $P(Tree(A))$ encompasses all possible subsets of the graph-tree.

All node sets of the *TreeSoft Set of level m* are:

$$Tree(A) = \{A_{i1} | i1 = 1, 2, \dots\}$$

The sets within the TreeSoft Set correspond to nodes at each level of the graph-tree: the first set consists of nodes at level 1, the second set consists

of nodes at level 2, and so on, up to the last set comprising nodes at level m . If the graph-tree has only two levels ($m = 2$), then the TreeSoft Set simplifies to a MultiSoft Set [Smarandache, 2018].

In summary, the TreeSoft Set provides a structured approach for representing and analyzing complex systems with hierarchical attributes. By incorporating a hierarchical organization, it enhances the flexibility and expressiveness of Soft Set-based methodologies, enabling more nuanced modeling and analysis of multi-level systems across various domains.

An illustrative example of a classical tree is shown in Fig.1.

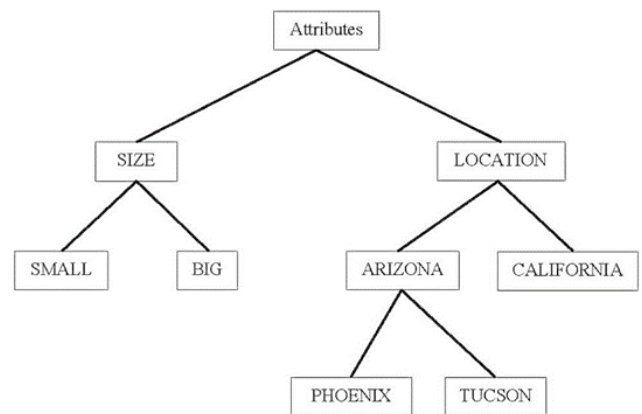


FIGURE 1. Schematic representation of the TreeSoft Set of Level 3 framework, illustrating the incorporation of hyperparameters to capture complex relationships within biomedical datasets.

This tree contains three levels as followed:

Level 0 (the root) is the node Attributes;

Level 1 is formed by the nodes: Size, Location;

Level 2 is formed by the nodes Small, Big, Arizona, and California;

Level 3 is formed by the nodes Phoenix, Tucson.

Let's consider $H = \{h_1, h_2, \dots, h_{10}\}$ be a set of houses, and $P(H)$ the power set of H .

And the set of Attributes: $A = \{A_1, A_2\}$, where $A_1 = \text{Size}$, $A_2 = \text{Location}$.

Then $A_1 = \{A_{11}, A_{12}\} = \{\text{Small}, \text{Big}\}$, $A_2 = \{A_{21}, A_{22}\} = \{\text{Arizona}, \text{California}\}$ as American states.

Further on, $A_{22} = \{A_{211}, A_{212}\} = \{\text{Phoenix, Tucson}\}$ as Arizonian cities.

Let's assume that the function F gets the following values:

$$F(\text{Big, Arizona, Phoenix}) = \{h_9, h_{10}\}$$

$$F(\text{Big, Arizona, Tucson}) = \{h_1, h_2, h_3, h_4\}$$

$F(\text{Big, Arizona}) = \text{all big houses from both cities, Phoenix and Tucson}$

$$= F(\text{Big, Arizona, Phoenix}) \cup F(\text{Big, Arizona, Tucson}) = \{h_1, h_2, h_3, h_4, h_9, h_{10}\}.$$

The TreeSoft Set introduces a hierarchical structure to Soft Set methodologies, enabling the representation and analysis of complex biological data in a hierarchical manner. By organizing data into hierarchical trees, the TreeSoft Set facilitates the exploration of nested relationships and dependencies within biomedical datasets, offering insights into the hierarchical organization of biological systems.

IV. PILOT STUDY

V. DISCUSSION

While the extensions of Soft Sets, such as HyperSoft Set, SuperHyperSoft Set, IndetermSoft Set, IndetermHyperSoft Set, and TreeSoft Set, offer significant advancements in modeling complex systems and handling uncertainty within biomedical data analysis, several unresolved aspects warrant further exploration:

- *Integration of Extensions:* Although each extension provides unique capabilities and applications, there is a need to explore how these extensions can be integrated synergistically to address multifaceted challenges in biomedical research. Investigating the interoperability and complementary nature of different Soft Set extensions could lead to more comprehensive methodologies for data analysis and decision-making, thereby enhancing the accuracy and reliability of diagnostics and personalized treatments.

- *Handling Complex Relationships:* While HyperSoft Sets and TreeSoft Sets enable the representation of complex relationships among attributes, there remains a challenge in effectively managing and analyzing these intricate networks. Future research should focus on developing advanced algorithms and techniques for extracting meaningful insights from interconnected data structures, particularly in the context of biomedical datasets characterized by multi-level

dependencies. By understanding and modeling these complex relationships, clinicians and researchers can gain deeper insights into disease mechanisms and treatment responses, ultimately improving diagnostics and personalized treatment strategies.

- *Quantification of Indeterminacy:* The presence of indeterminate data in IndetermSoft Sets and IndetermHyperSoft Sets poses challenges in quantifying and interpreting uncertainty. Further investigations are needed to develop robust methodologies for measuring and representing different degrees of indeterminacy, enhancing the reliability and interpretability of results derived from these frameworks. By accurately quantifying uncertainty, clinicians can make more informed decisions regarding diagnosis and treatment selection, taking into account the inherent variability and ambiguity present in biomedical data.

- *Scalability and Efficiency:* As biomedical datasets continue to grow in size and complexity, there is a pressing need for scalable and efficient algorithms capable of handling large-scale data analysis tasks. Research efforts should focus on optimizing computational techniques and resource allocation strategies to ensure the scalability and efficiency of Soft Set-based methodologies in real-world applications. By improving the scalability and efficiency of data analysis techniques, clinicians and researchers can analyze large datasets more effectively, leading to faster and more accurate diagnostics and personalized treatment recommendations.

- *Validation and Benchmarking:* Despite the theoretical advancements in Soft Sets and their extensions, there is a lack of comprehensive validation frameworks and benchmark datasets for evaluating the performance of these methodologies. Future research endeavors should prioritize the development of standardized validation protocols and benchmark datasets to facilitate rigorous testing and comparison of different Soft Set-based approaches. By validating Soft Set-based models using standardized protocols and benchmark datasets, clinicians and researchers can ensure the reliability and generalizability of diagnostic and treatment recommendations derived from these methodologies.

- *Interpretability and Transparency:* Enhancing the interpretability and transparency of Soft Set-based models is crucial for fostering trust and adoption in biomedical research and clinical practice. Researchers should explore techniques for explaining model decisions and capturing the

underlying uncertainty in a transparent manner, enabling stakeholders to understand and trust the insights derived from these methodologies. By improving the interpretability and transparency of Soft Set-based models, clinicians can better understand the rationale behind diagnostic and treatment recommendations, leading to increased confidence in personalized treatment strategies and ultimately improving patient outcomes.

VI. CONCLUSION

The evolution and adoption of Soft Sets and their various extensions, including the HyperSoft Set, IndetermSoft Set, IndetermHyperSoft Set, and TreeSoft Set, represent a significant leap forward in computational methodologies, particularly within the realm of bioinformatics. These extensions provide novel avenues for modeling and analyzing complex biological datasets, which are often plagued by uncertainty, imprecision, and vagueness.

In the context of bioinformatics, where data are diverse and frequently noisy or incomplete, the adaptability and versatility of Soft Sets and their variants prove invaluable. They offer researchers the means to navigate the inherent uncertainties present in biological data, such as those arising from gene expression profiles, protein interactions, and metabolic pathways. By embracing the inherent fuzziness and imprecision of biological phenomena, Soft Sets empower researchers to conduct more accurate and robust analyses, thus uncovering deeper insights into biological systems.

Moreover, the flexibility of Soft Sets enables seamless integration with other computational techniques and algorithms commonly employed in bioinformatics. This integration amplifies their utility, allowing researchers to combine the strengths of Soft Sets with established methods, thereby enriching analyses and bolstering decision-making processes.

In conclusion, Soft Sets and their extensions play a pivotal role in bioinformatics, offering a versatile framework to tackle the complexities and uncertainties inherent in biological data. Through their application, these methodologies drive innovation, deepen our understanding of biological systems, and ultimately contribute to advancements in human health and well-being. Our analysis underscores the efficacy of Soft Sets and their extensions in handling the intricacies of biomedical data, enabling more accurate predictions and facilitating insightful discoveries that propel biomedical research forward.

ACKNOWLEDGMENTS

We are grateful to editors and reviewers, as well as the correspondent author, who offered assistance in the form of advice, assessment, and checking during the study period.

REFERENCES

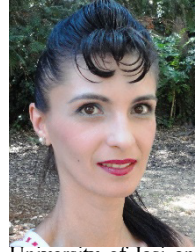
- [1] D. Gîfu, D. Trandabăț, K. Cohen, J. Xia, "Special Issue on the Curative Power of Medical Data". *Data*, 4(2), 85, 2019, DOI: 10.3390/data4020085.
- [2] D. Thesmar, D. Sraer, L. Pinheiro, N. Dadson, R. Veliche, P. Greenberg, "Combining the Power of Artificial Intelligence with the Richness of Healthcare Claims Data: Opportunities and Challenges". *PharmacoEconomics* 37, 745–752, 2019. DOI: 10.1007/s40273-019-00777-6.
- [3] D. Molodtsov, "Soft Set Theory First Results". *Computer Math. Applic.* 37:19-31, 1999.
- [4] F. Smarandache, D. Gîfu and M. Teodorescu, "Neutrosophic Elements in Discourse". *Social Sciences and Education Research Review*, 2/1: 25-32, 2015.
- [5] D. Gifu, "AI-backed OCR in Healthcare". *Procedia Computer Science*, open access journal, ELSEVIER, 207:1134–1143, 2022, DOI: 10.1016/j.procs.2022.09.169.
- [6] F. Smarandache, "Extension of Soft Set to Hypersoft Set, and then to Plithogenic Hypersoft Set". *Neutrosophic Sets and Systems*, 22:168-170, 2018, DOI: 10.5281/zenodo.2159754; <http://fs.unm.edu/NSS/ExtensionOfSoftSetToHypersoftSet.pdf>
- [7] F. Smarandache, "Extension of Soft Set to Hypersoft Set, and then to Plithogenic Hypersoft Set (revisited)". *Octagon Mathematical Magazine*, 27(1):413-418, 2019
- [8] F. Smarandache, "Introduction to the IndetermSoft Set and IndetermHyperSoft Set". *Neutrosophic Sets and Systems*, 50:629-650, 2022, DOI: 10.5281/zenodo.6774960; <http://fs.unm.edu/NSS/IndetermSoftIndetermHyperSoft38.pdf>.
- [9] F. Smarandache, "Neutrosophic Function, in Neutrosophic Precalculus and Neutrosophic Calculus", Brussels, 14-15, 2015,

- <http://fs.unm.edu/NeutrosophicPrecalculusCalculus.pdf>.
- [10] F. Smarandache, "Neutrosophic Function, in Introduction to Neutrosophic Statistics", Sitech & Education Publishing, 74-75, 2014, <http://fs.unm.edu/NeutrosophicStatistics.pdf>.
- [11] F. Smarandache, "Soft Set Product extended to HyperSoft Set and IndetermSoft Set Product extended to IndetermHyperSoft Set". *Journal of Fuzzy Extension and Applications*, 2022, DOI: 10.22105/jfea.2022.363269.1232, http://www.journal-fea.com/article_157982.htm.
- [12] S. Alkhazaleh, A. R. Salleh, A. Razak, N. Hassan, A. G. Ahmad, "Multisoft Sets". *Proc. 2nd International Conference on Mathematical Sciences*, 910-917, 2010, Kuala Lumpur, Malaysia.
- [13] A. Alqazzaz, and K. M. Sallam, "Evaluation of Sustainable Waste Valorization using TreeSoft Set with Neutrosophic Sets". *Neutrosophic Sets and Systems* 65, 1 (2024). https://digitalrepository.unm.edu/nss_journal/vol65/iss1/9
- [14] F. Smarandache, "Introduction to the IndetermSoft Set and IndetermHyperSoft Set". *Neutrosophic Sets and Systems*, Vol. 50, 629-650, 2022. Available at SSRN: <https://ssrn.com/abstract=4317100>
- [15] G. Dhanalakshmi, S. Sundarr, F. Smarandache, "Selection of the Best Process for Desalination Under a Treesoft Set Environment Using the Multi-criteria Decision-making Method". *International Journal of Neutrosophic Science*, Vol. 23, 140-147, 2024. 10.54216/IJNS.230312.
- [16] P. Maji, R. Biswas, A. R. Roy, "Intuitionistic Fuzzy Soft Sets". *The Journal of Fuzzy Mathematics*, Vol. 9(3), 2001.
- [17] L. A. Zadeh, "Fuzzy Sets and Their Application to Pattern Classification and Clustering Analysis". *Classification and Clustering*, Editor(s): J. Van Ryzin, Academic Press, 1977, 251-299, DOI: 10.1016/B978-0-12-714250-0.50014-0.
- [18] H.-J. Zimmermann, L.A. Zadeh, B.R. Gaines, "Fuzzy Sets and Decision Analysis", Elsevier, 1984.
- [19] P. Majumdar P., S.K. Samanta, "Similarity Measure of Soft Sets". *New Math. Nat. Comput.* 4:1-12, 2008.
- [20] P. Majumdar P., S.K. Samanta, "On Similarity and Entropy of Neutrosophic Sets". *J. Intell Fuzzy Syst.*, 26:1245-1252, 2014.
- [21] F. Smarandache, Abdel-Basset (eds.), "Neutrosophic Sets and Systems", Vol. 32, University of New Mexico, Educational Publisher Inc., Ohio, USA, 2020
- [22] K. Atanassov, "Intuitionistic fuzzy sets". *Fuzzy Sets and Systems*; 20, 87-96, 1986.
- [23] Y. Zou, Y. and Z. Xiao, "Data Analysis Approaches of Soft Sets Under Incomplete Information". *Knowledge Based Systems*, 21, 941-945, 2008.
- [24] M. Naz, and M. Shabir, "On Fuzzy Bipolar Soft Sets, Their Algebraic Structures and Applications", 1645-1656, 1 Jan. 2014.
- [25] D. Gîfu, "Malaria Detection System". *Proceedings of the International Conference on Mathematical Foundations of Informatics*, MFOI-2017, Cojocaru, S. and Gaiandric, C., Druguş, I. (eds.), Institute of Mathematics and Computer Science, Academy of Sciences of Moldova, Chişinău, 74-78, 2017.
- [26] D. Gîfu, D. Trandabăţ, K. Cohen, J. Xia, "Special Issue on the Curative Power of Medical Data". *Data*, 4(2), 85, 2019, DOI: 10.3390/data4020085.
- [27] D. Gîfu, "The Use of Decision Trees for Analysis of the Epilepsy." *Procedia Computer Science*, open access journal, 192: 2844-2853, 2021.
- [28] F. Smarandache, "Foundation of the SuperHyperSoft Set and the Fuzzy Extension SuperHyperSoft Set: A New Vision". *Neutrosophic Systems with Applications*, Vol. 11, 48-51, 2023.



FLORENTIN SMARANDACHE received the M.Sc. degree in mathematics and in computer science from the University of Craiova, Romania, and the Ph.D. degree in mathematics from the State University of Kishinev. He completed his postdoctoral research in applied mathematics from Okayama University of Sciences, Japan, and The Guangdong University of Technology, Guangzhou, China. He is currently an Emeritus Professor in mathematics with The University of

New Mexico, USA. He has been the Founder of Neutrosophy (generalization of dialectics), neutrosophic set, logic, probability, and statistics, since 1995, and has published 100's of papers and books on neutrosophic physics, super lumina land instantaneus physics, unmatter, quantum paradoxes, also late theory of relativity, redshift and blueshift due to the medium gradient and refraction index besides the Doppler effect, paradoxism, outerart, neutrosophy as a new branch of philosophy, law of included multiple-middle, multispace and multistructure, HyperSoft set, TreeSoft set, IndetermSoft set and IndetermHyperSoft set, SuperHyperGraph, SuperHyperTopology, SuperHyperAlgebra, SuperHyperFunction, Neutrosophic SuperHyperAlgebra, degree of dependence and independence between neutrosophic components, refined neutrosophic set, neutrosophic over-under-off-set, plithogenic set/logic/probability/statistics, symbolic plithogenic algebraic structures, neutrosophic triplet and duplet structures, quadruple neutrosophic structures, extension of algebraic structures to NeutroAlgebra and AntiAlgebra, NeutroGeometry and AntiGeometry, NeutroTopology and AntiTopology, refined neutrosophic topology, refined neutrosophic crisp topology, and dezer-smarandache theory to many peer-reviewed international journals and many books. He presented papers and plenary lectures to many international conferences around the world. In addition, he has published many books of poetry, dramas, children's stories, translations, essays, a novel, folklore collections, traveling memories, and art albums. For more information visit the link: <https://fs.unm.edu/FlorentinSmarandache.htm>.



DANIELA GIFU was born in Barlad Village, Vaslui County, Romania, in 1973. She received a Ph.D. in Computer Science in 2016 and a Ph.D. in Philosophy in 2010 from the "Alexandru Ioan Cuza" University of Iasi, Romania. From 2010 to 2013, she was a postdoctoral researcher at the Computational Linguistics Laboratory. Since 2013, she has been an affiliate associate professor and scientific researcher with the Computer Science Department at the "Alexandru Ioan Cuza"

University of Iasi and other Romanian universities. Dr. Gifu is the (co-)author of 19 books, more than 250 articles, and over a dozen linguistics resources and tools for public discourse analysis. Her main research interests include the semantic web, service computing, and machine learning. Her research mainly focuses on sentiment analysis in social media and machine learning. She also serves as an Associate Editor for eight journals in the field of computer science and holds a pending patent approval. In 2023, Dr. Daniela Gifu was honored with the Diploma of Gold Medal at the 2nd International Exhibition of Innovation and Technology Transfer EXCELLENT IDEA in Chisinau, Moldova. For more information visit the link: <https://profs.info.uaic.ro/daniela.gifu>